Thermonuclear Burst Oscillations

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Abstract

Burst oscillations, a phenomenon observed in a significant fraction of Type I (thermonuclear) X-ray bursts, involve the development of highly asymmetric brightness patches in the burning surface layers of accreting neutron stars. Intrinsically interesting as nuclear phenomena, they are also important as probes of dense matter physics and the strong gravity, high magnetic field environment of the neutron star surface. Burst oscillation frequency is also used to measure stellar spin, and doubles the sample of rapidly rotating (above 10 Hz) accreting neutron stars with known spins. Although the mechanism remains mysterious, burst oscillation models must take into account thermonuclear flame spread, nuclear processes, rapid rotation, and the dynamical role of the magnetic field. This review provides a comprehensive summary of the observational properties of burst oscillations, an assessment of the status of the theoretical models that are being developed to explain them, and an overview of how they can be used to constrain neutron star properties such as spin, mass, and radius.

Keywords

binaries: general, stars: neutron, stars: rotation, X-rays: bursts
1. INTRODUCTION

Type I X-ray bursts are thermonuclear explosions triggered by unstable burning in the oceans of accreting neutron stars. The ocean is the low-density fluid layer of light elements that builds up via accretion on top of the solid crust (see Chamel & Haensel 2008 for a discussion of the conditions under which a Coulomb plasma of ions crystallizes to form a solid). The basic cause of bursts, an imbalance between nuclear heating and radiative cooling in settling material, can be explained using simple one-dimensional calculations (for reviews, see Lewin, van Paradijs & Taam 1993 and Bildsten 1998b). The past decade, however, has revealed major complexities that can no longer be understood within the context of such simple models (Strohmayer & Bildsten 2006).

One such complexity is the development of asymmetric brightness patches, known as burst oscillations, in about 10% of the bursts observed with high time resolution instrumentation (Galloway et al. 2008). What drives this process remains unexplained and requires us to consider flame spreading and other multidimensional effects. The highly atypical properties of burst oscillations from the accretion-powered pulsars also suggest an important dynamical role for the magnetic field. This review provides an overview of our current understanding of burst oscillations: the techniques employed to detect and analyze them, their key observational properties, the status of theoretical models, and the ways in which they can be used to constrain stellar spin rates and the dense matter equation of state.

1.1. Burst Oscillations: A Brief History

Although a number of searches for periodic phenomena in X-ray bursts were carried out prior to the mid-1990s, and some tentative detections were claimed, none have stood the test of time (Lewin, van Paradijs & Taam 1993; Jongert & van der Klis 1996). Conclusive detection of strong periodic signals in thermonuclear bursts came only with the launch of the Rossi X-ray Timing Explorer (RXTE) on December 30, 1995.

Observations of the burster 4U 1728-34 in February 1996, only weeks after the start of science operations, led to the discovery of a strong 363-Hz signal in six X-ray bursts (Strohmayer et al. 1996). These researchers dubbed this phenomenon burst oscillations. Many of the properties that we now consider hallmarks of burst oscillations were apparent even in these first observations: high coherence, an upward drift of \( \sim 1 \) Hz toward an asymptotic maximum frequency as the burst progressed, amplitudes of up to \( \sim 10\% \) root mean square (rms), and the apparent disappearance of the signal during the burst peak.

Strohmayer et al. (1996) concluded that rotational modulation of a bright spot on the burning surface was the most likely explanation for the burst oscillations. This was based on three arguments: the expected evolutionary link between accreting neutron stars in low-mass X-ray binaries and the millisecond radio pulsars (with the former being progenitors of the latter via the spin recycling scenario, see Bhattacharya & van den Heuvel 1991); the ability of a localized hot spot to explain the observed amplitudes; and the high coherence of the oscillations seen in the burst tails.

Between 1996 and 2002, burst oscillations were discovered in bursts from eight more sources (see Table 1). Although there was still no independent confirmation of spin rate, the link between burst oscillation frequency and stellar rotation was nonetheless strengthened. The facts that the same frequency was seen in multiple bursts from any given source and the asymptotic frequency of the drifting burst oscillations had high stability both pointed to rotational modulation of a bright spot that was near stationary in the rotating frame of the star (Strohmayer et al. 1998a, Muno et al. 2002). The detection of burst oscillations during a superburst (a longer, more energetic burst thought to be due to unstable carbon burning) from 4U 1636-536 also supported...
<table>
<thead>
<tr>
<th>Source</th>
<th>Frequency (Hz)</th>
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<tr>
<td>Persistent accretion-powered pulsars with burst oscillations</td>
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<tr>
<td>SAX J1808.4-3658</td>
<td>401</td>
<td>Chakrabarty et al. (2003)</td>
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<td>Strohmayer et al. (2003)</td>
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<td>IGR J17511-3037</td>
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<td>Altamirano et al. (2010b)</td>
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<td>IGR J17480-2446</td>
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<td>Intermittent accretion-powered pulsars with burst oscillations</td>
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<td>Aql X-1</td>
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<td>Zhang et al. (1998)</td>
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<td>HETE J1900.1-2455</td>
<td>377</td>
<td>Watts et al. (2009)b</td>
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<td>Burst oscillation sources without detectable accretion-powered pulsations</td>
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<tr>
<td>4U 1608-522</td>
<td>620</td>
<td>Hartman et al. (2003), Galloway et al. (2008)</td>
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<td>Kaaret et al. (2002), Galloway et al. (2008)</td>
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<td>GRS 1741.9-2853</td>
<td>589</td>
<td>Strohmayer et al. (1997)</td>
</tr>
<tr>
<td>X 1658-298</td>
<td>567</td>
<td>Wijnands, Strohmayer &amp; Franco (2001)</td>
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<tr>
<td>EXO 0748-676</td>
<td>552</td>
<td>Galloway et al. (2010a)</td>
</tr>
<tr>
<td>KS 1731-260</td>
<td>524</td>
<td>Smith, Morgan &amp; Bradt (1997); Muno et al. (2000)</td>
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<td>4U 1728-34</td>
<td>363</td>
<td>Strohmayer et al. (1996)</td>
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<tr>
<td>4U 1702-429</td>
<td>329</td>
<td>Markward, Strohmayer &amp; Swank (1999)</td>
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<tr>
<td>IGR J17191-2821</td>
<td>294</td>
<td>Altamirano et al. (2010a)</td>
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</tbody>
</table>

*Second (confirmation) references are given for sources where the initial discovery rested on a single burst (but see also note b). Although burst oscillations from this source have only been detected in a single burst, they were observed in multiple independent time bins. We therefore consider this detection to be secure.*

this interpretation. The frequency matched that seen in the normal Type I bursts despite the different burst physics, suggesting an external clock (Strohmayer & Markwardt 2002).

In October 2002, the 401-Hz accretion-powered millisecond X-ray pulsar SAX J1808.4-3658 went into outburst, and Chakrabarty et al. (2003) reported the first robust detection of burst oscillations from a source with an independent measure of the spin rate (analysis of a burst during a previous accretion episode had yielded a marginal detection; in’t Zand et al. 2001). Although the frequency of the burst oscillations drifted by several hertz in the burst rise, the frequency in the tail was within $\approx 6 \times 10^{-3}$ Hz of the spin frequency. A second accretion-powered pulsar with
burst oscillations at the spin frequency, XTE J1814-338, followed shortly thereafter (Strohmayer et al. 2003), confirming the status of burst oscillation sources as nuclear-powered pulsars. Since this time, burst oscillations have been found in several additional sources (Table 1), including three more accretion-powered pulsars and two intermittent pulsars (sources that show accretion-powered pulsations only sporadically). Although rotational modulation of a brightness asymmetry on the burning surface remains an integral part of all models, the root cause of such an asymmetry remains unresolved.

2. BURST OSCILLATION OBSERVATIONS

2.1. Principles of Detection

The standard analysis technique, when searching for periodic or quasi-periodic signals, is to use fast Fourier transforms to produce a power spectrum. For a comprehensive review of this topic, the reader is referred to van der Klis (1989). Here, I summarize only the key points that are essential to an understanding of burst oscillation detection (this is of particular relevance to the discussion in Table 2 about tentative detections) and subsequent analysis of properties like frequency and amplitude.

A series of X-ray photon arrival times with total duration $T$ is binned to form a time series $x_k(t_k)$, the number of photons (counts) in time bin $t_k$ ($k = 1, \ldots, N$). The time resolution $\Delta t = T/N$ is limited by the native time resolution of the instrument (typically 1–125 $\mu$s for RXTE, depending on data mode), but is also set by the desired Nyquist frequency $f_{Ny}$. This is the maximum frequency that can be studied for a given time resolution and is given by $f_{Ny} = 1/(2\Delta t)$. The power spectrum $P_j$ at the Fourier frequencies $\nu_j = j/T$ ($j = 0, 2, \ldots, N/2$, where $v_{N/2} = f_{Ny}$), using the standard Leahy normalization (Leahy et al. 1983), is then given by

$$P_j = \frac{2}{N\gamma} \left[ \left( \sum_{j=1}^{N} x_k \cos 2\pi \nu_j t_k \right)^2 + \left( \sum_{j=1}^{N} x_k \sin 2\pi \nu_j t_k \right)^2 \right],$$

where $N\gamma$ is the total number of photons.

In the absence of any deterministic signal, the Poisson statistics of photon counting yield powers that are distributed as $\chi^2$ with two degrees of freedom (d.o.f.). The presence of a periodic signal at a given frequency boosts the power in the appropriate frequency bin. If we detect a large power, however, we must first evaluate its significance by computing the probability of obtaining such a high value of the power, in the absence of a periodic signal, due to the natural fluctuations in powers that are a by-product of photon counting statistics. We compute this using the known properties of the $\chi^2$ distribution, taking into account the numbers of trials (see below).

Many burst oscillation papers use the $Z^2$ statistic, instead of the power spectrum. Although very similar to the standard power spectrum computed from a Fourier transform, it does not require that the photon arrival times be binned. It is defined as

$$Z^2 = \frac{2}{N\gamma} \sum_{k=1}^{n} \left[ \left( \sum_{j=1}^{N\gamma} \cos k\phi_j \right)^2 + \left( \sum_{j=1}^{N\gamma} \sin k\phi_j \right)^2 \right],$$

where here $n$ is the number of harmonics (most commonly taken to be 1), $k = 1, 2, \ldots, n$ is the index used to sum over harmonics, $N\gamma$ is the total number of photons, and $j$ is an index applied to
each photon. The phase $\phi_j$ for each photon is defined as

$$\phi_j = 2\pi \int_{t_0}^{t_j} \nu(t)dt,$$

where $\nu(t)$ is the frequency under consideration and $t_j$ is the arrival time of each photon relative to some reference time $t_0$. Frequency $\nu(t)$ is most commonly taken to be constant (so that it can be taken outside the integral) but on occasion may be a function of time, for example, if one wants

<table>
<thead>
<tr>
<th>Table 2</th>
<th>Sources with single burst or tentative burst oscillation detections$^a$</th>
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<tbody>
<tr>
<td>Source</td>
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<td>MXB 1730-335</td>
<td>306</td>
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<td>4U 1916-053</td>
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<td>XB 1254-690</td>
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(Continued)
Table 2 (Continued)

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<tr>
<th>Source</th>
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<th>Remarks</th>
</tr>
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<tbody>
<tr>
<td>EXO 0748-676</td>
<td>45</td>
<td>Villarreal &amp; Strohmayer (2004) report a (\sim 5.5\sigma) signal after stacking power spectra from the tails of 38 bursts. Significance was estimated by fitting the distribution of measured powers, taking into account the number of frequency bins searched. Since this time, strong burst oscillations at 552 Hz have been discovered in this source (Galloway et al. 2010a and Table 1). Galloway et al. (2010a) confirm the detection of the 45-Hz feature in the sample used by Villarreal &amp; Strohmayer (2004), but do not find it when using a larger sample of bursts. Its nature remains unclear.</td>
</tr>
</tbody>
</table>

aThe table gives the significance quoted by the researchers for the candidate detection and explains the methods used to derive this significance. As explained in Section 2.1, estimates derived using \(\chi^2\) with 2 d.o.f. rather than Monte Carlo simulations tend to overestimate significance. The procedure for estimating the number of trials varies from paper to paper: Ideally, proper allowance should be made for the number of bursts, energy bands, frequency bins, and time windows searched. The SAX J1748.9-2021 result is particularly informative in terms of illustrating the importance of using the correct number of trials. Whether to give equal weight in terms of numbers of trials to every burst searched remains a matter of debate. The number of Rossi X-ray Timing Explorer (RXTE) proportional counter units active during observations varies (with more photons maximizing detection chances), and in addition burst oscillations tend to occur preferentially in certain accretion states (see Section 2.3.2).

To correct for smearing due to orbital Doppler shifts as the neutron star orbits the center of mass of the binary. In the absence of a deterministic (e.g., periodic) signal, \(Z^2\) is distributed as \(\chi^2\) with \(2n\) d.o.f. An advantage of \(Z^2\) is that it offers an efficient way of summing harmonics.

When searching for drifting, or quasi-periodic signals, it is common to average powers from neighboring frequency bins. In searches for weak signals, one can also stack, or take an average of, power spectra from many independent data segments (time windows) or bursts. This affects the number of d.o.f. in the theoretical \(\chi^2\) distribution of noise powers, but the modified theoretical distribution is known (see van der Klis 1989 for more details).

To assess whether a periodic signal is indeed present, we first take the power spectrum and identify the frequency bins with the highest powers. One then computes the probability of obtaining such high powers through Poisson noise alone, using the properties of the \(\chi^2\) distribution with the appropriate number of degrees of freedom. One must then take into account the number of trials that have been made—the more trials, the more likely one is to obtain a high power via statistical fluctuations alone. The number of trials is the product of the number of independent frequency bins, time windows, energy bands, bursts, and (if appropriate) sources searched. Assessing the number of trials properly is complicated by the fact that many burst oscillation searches use overlapping time bins or oversampled frequency bins to maximize candidate signal power. Failure to account properly for this can result in the significance of a candidate signal being overestimated (or underestimated, if overlapping bins are treated as being independent). If the probability of such a high value of the power arising through Poisson noise alone is below a certain threshold after taking into account numbers of trials, then it is deemed significant, with the quoted significance referring to the chances of having obtained such a signal through Poisson noise alone.

A complication comes from the fact that noise powers (the power distribution in the absence of a periodic signal) are not always distributed in accordance with the \(\chi^2\) that would be expected from constant Poisson noise. What we are searching for in an X-ray burst is a periodic signal superimposed on the overall deterministic rise and decay of a burst lightcurve. These variations give low-frequency power and add sidebands to noise powers, boosting their level (for a nice discussion of these issues, see Fox et al. 2001). This problem is particularly acute in the rising phase of the burst when the lightcurve is changing rapidly. There may also be other noise components from astrophysical or detector processes, such as red noise associated with accretion, which may continue during the burst and contribute to the overall emission.
Assessing the true distribution that the powers should take, in the absence of a periodic signal, is most easily done using Monte Carlo simulations. One can, for example, make a model of the burst lightcurve by fitting the rise and decay with exponential functions, and then use this as a basis to generate a large sample of fake lightcurves with Poisson counting statistics but without any periodic signals. Taking power spectra from these fake lightcurves then yields the true, most likely frequency-dependent, distribution of noise powers. One other advantage of the Monte Carlo method is that any peculiarities of the data analysis process (such as the use of overlapping time windows) can be replicated precisely. As a rule of thumb, unless a candidate signal is particularly strong, or is repeated in multiple independent bursts or time windows (thereby boosting significance), Monte Carlo simulations should really be done to obtain an accurate assessment of significance. Alternatively, one can also try to fit the distribution of measured powers (excluding the frequency bins containing the candidate signals); however, this is somewhat risky because it, by definition, excludes extreme values from the fit.

One final factor that must be considered, for the accretion-powered pulsars with burst oscillations, is the likely continuation of the channeled accretion process during the burst. One must therefore ask whether the signal detected during the burst could be due to the accretion-powered pulsations. If the accretion process (accretion rate and fractional amplitude of accretion-powered pulsations) remains unchanged during the burst, the addition of a large number of unpulsed photons during the burst would cause the measured fractional amplitude to fall (by a factor of $N_{\text{bur}} / N_{\text{acc}}$, where $N_{\text{bur}}$ is the number of photons due to burst emission and $N_{\text{acc}}$ is the number due to accretion in the data segment being considered). In all cases so far, fractional amplitudes remain similar despite the fact that burst flux far exceeds accretion flux, indicating that the burst emission itself must also be pulsed (provided that the assumption of unchanged accretion holds). Whether this assumption is reasonable remains a matter of debate. Naively, one might expect radiation pressure from a burst to hinder the accretion process. However, the radiation may also remove angular momentum, thus increasing the accretion rate (Walker & Meszaros 1989, Miller & Lamb 1993, Ballantyne & Everett 2005).

### 2.2. Measurable Properties

Once a burst oscillation signal has been identified and deemed statistically significant, one can measure several observational properties. Some properties can be calculated directly from the power spectrum or $Z_2^\nu$ statistic (for the rest of this subsection, these two terms can be used interchangeably), whereas others require pulse profile modeling. The latter technique involves selecting a frequency model for the signal, $\nu(t)$, and calculating a phase for each photon using Equation 3, using this to assign each photon to a phase bin, and thereby building up a pulse profile (number of photons per phase bin). The main intrinsic properties of interest are frequency, amplitude, and phase lags. The first two can be measured from the power spectrum or using pulse profile modeling, but to obtain phase lags one must use pulse profile modeling because the power spectrum discards phase information.

In terms of frequency, we are interested in both the absolute value and the properties of any drift. The latter is most commonly visualized using dynamical power spectra. These are computed by taking power spectra of short, usually overlapping, segments of data from the burst lightcurve, as illustrated in Figure 1. The power spectra are then commonly plotted as contours, overlaid on the burst lightcurve. Several examples of bursts with oscillations, from different sources, are shown in Figure 2. One can then see the frequency drift that occurs as the burst progresses. Another property, related to frequency, that is often given is the coherence $Q$ of the burst oscillation train.
Figure 1

Generating a dynamical power spectrum. (a) The burst lightcurve (dark yellow line) is first split into segments. In this case, there are three overlapping time windows, $\Delta t_0$, $\Delta t_1$, and $\Delta t_2$. The time stamps $T_0$, $T_1$, and $T_2$ refer to the midpoints of each window. (b) Computing a power spectrum for each segment, one can see that both power and frequency vary with time (blue, low power; purple, medium power; red, high power). (c) This can be plotted in power-frequency-time space. The resulting contours of power (purple, medium; red, high) are projected onto the frequency-time plane, and (d) the resulting dynamical power spectrum is overplotted on the lightcurve.

This is given by

$$Q = \frac{v}{\Delta_{\text{FWHM}}}.$$  \hspace{1cm} (4)

where $v$ is the frequency of the peak in the power spectrum and $\Delta_{\text{FWHM}}$ is its full width at half-maximum, obtained by fitting a Gaussian or Lorentzian function to the broad peak in the power spectrum. Note that $Q$ values are often quoted for peaks where the frequency drift has been incorporated into the model (as in Equation 3), thereby rendering the peak in the power spectrum narrower and, hence, more coherent (see, for example, Strohmayer & Markwardt 1999). In this case, the frequency $v$ that is used in computing $Q$ is normally the asymptotic maximum frequency (Sections 1 and 2.3.3).

The amplitude of the pulsations can be computed directly from the power spectrum or from a folded pulse profile (see, for example, Muno, Özel & Chakrabarty 2002 and Watts, Strohmayer 2002).
When using the power spectrum, the rms fractional amplitude $r$ is given by

$$r = \left( \frac{P}{N_v} \right)^{1/2} \left( \frac{N_v}{N_v - N_b} \right),$$

where $P$ is the signal power, $N_v$ the total number of photons, and $N_b$ the number of background photons (estimated from the period before or after the burst). Note that signal power is not the same as the measured power. Once a power has been deemed significant (i.e., unlikely to have occurred through noise alone), one must then determine the signal power that would give rise to the measured value because measured power includes the effects of noise (Groth 1975). For details of how to compute signal power from measured power, see Vaughan et al. (1994), Muno, Özel & Chakrabarty (2002), or Watts, Strohmayer & Markwardt (2005). For sources that also have accretion-powered pulsations, this value is often corrected to remove the expected contribution.
due to continuing pulsed accretion during the burst. Other related quantities that can be computed are the amplitudes of any higher harmonics of the burst oscillation frequency (often referred to as the harmonic content), and the dependence of the amplitude on photon energy.

There are several factors to be wary of when using values of amplitude from the literature. Different groups use different definitions of amplitude: For a lightcurve that varies as \( C + A \sin 2\pi vt \), different groups may quote, for the signal at frequency \( v \), full fractional amplitude \((2A/C)\), half fractional amplitude \((A/C)\), or rms fractional amplitude \((A/C\sqrt{2})\). In addition, amplitude depends on the frequency model used. Fitting apparent frequency drift increases amplitude, but this must be taken into account when testing models because the two are not independent. The third factor, specific to the power spectrum technique, is that amplitude is suppressed when frequency drifts between Fourier bins (van der Klis 1989). This effect can sometimes be seen in published dynamical power spectra: Compare, for example, the dynamical power spectra in figure 1 of Munoz, Ozel & Chakrabarty (2002) with those in figure 1 of Watts et al. (2009), where an interbin response function is used to reduce the effects of this drop [although note that this does not affect the amplitudes in Munoz, Ozel & Chakrabarty (2002), which were computed using folded pulse profiles].

Energy-dependent phase lags, which are of use when testing models, are computed by comparing pulse profiles constructed from photons in different energy bands. The degree to which the folded pulse profiles are offset is the phase lag. This type of analysis can also be used to compare the phases of burst oscillations to accretion-powered pulsations for sources that show both phenomena. Care must be taken when doing this to correct for any contamination due to the continued presence of accretion-powered pulsations during the burst. However, the magnitude of the correction is simple to estimate (see Watts, Patruno & van der Klis 2008).

Finally, one can analyze the dependence of the burst oscillation characteristics on the properties of the bursts and the accretion state of the star. Burst properties may include the total integrated flux (fluence), peak flux, the presence or absence of photospheric radius expansion, duration, and rise and decay timescales. In terms of accretion state, one can consider the overall accretion rate (which can be estimated in various ways) and, for the pulsars, compare the properties of the burst oscillations to those of the accretion-powered pulsations. Note that burst type also depends strongly on accretion rate, so these two factors are not unrelated.

2.3. Observational Properties

This section gives an overview of the main properties of burst oscillations and the sources that exhibit them, as established by astronomical observations. In addition to summarizing all confirmed and tentative detections, I review the conditions under which burst oscillations are observed to develop, and I discuss their signature characteristics including frequencies, frequency drifts, and (energy-dependent) pulse shapes.

2.3.1. Overview of burst oscillation sources. Secure detections of burst oscillations have now been made in 17 sources (Table 1), including 5 persistent accretion-powered pulsars and 2 intermittent accretion-powered pulsars. Note that all are transient accretors, and the use of the term persistent to describe the presence of accretion-powered pulsations through accretion episodes—as used here—should not be confused with its use to describe sources that are persistently, as opposed to transiently, accreting. All of the burst oscillation sources are in low-mass X-ray binaries (Tauris & van den Heuvel 2006) with orbital periods (where known) in the range of 1.4 to 19 hours. There is one candidate ultracompact binary in this group, 4U 1728-34, but the orbital period for this source is not known (see Galloway et al. 2010b). Ideally, for a detection to be secure,
the same frequency should have been seen in multiple bursts from the same source. For one of the sources in Table 1 this is not the case. In this case, the high statistical significance of the detection is based upon the fact that the same frequency was seen in multiple independent time bins within a single burst, which is very close to the spin frequency observed from accretion-powered pulsations.

Table 2 gives details of several other sources for which burst oscillation detections have been claimed. Some of the detections are very marginal (below the standard 3σ threshold), and most rely on a power in a single independent time bin in a single burst. Also given in the table is a summary of the analysis procedure used to estimate the significance of the claimed detection. Comparing these procedures to the ideal outlined in Section 2.1, the significance of some of these results has probably been overestimated. As such, they should be considered tentative until confirmed in a second burst.

### 2.3.2. Conditions in which burst oscillations are detected

For four of the five persistent pulsars, burst oscillations have been detected in all observed bursts, irrespective of burst properties or accretion state (see Table 1 for references)—although the persistent pulsars do not typically exhibit a wide range of accretion states. For the fifth persistent pulsar (IGR J17498-2921), oscillations have only been detected in the two brightest bursts. However, the upper limits on the presence of oscillations in the weaker bursts are comparable to the amplitudes detected in the brighter bursts (Chakraborty & Bhattacharyya 2012), so they could well be present at the same level in these other bursts. For the other sources (the nonpulsars and intermittent pulsars), burst oscillations are detected in only a subset of bursts.

A comprehensive analysis of burst and burst oscillation properties by Galloway et al. (2008) found that the properties of the bursts (e.g., duration or recurrence times) where oscillations are detected are not unusual compared to the properties of bursts where oscillations are not detected. There does, however, appear to be a correlation with accretion state, as estimated from the color-color diagram, which is a plot of hard-against-soft X-ray colors. As accretion rate increases, low-mass X-ray binaries typically move from the top left (hard) to bottom right (soft), tracing out a Z-shaped pattern (Hasinger & van der Klis 1989). The persistent pulsars, including those with burst oscillations, tend to remain in the hard (low accretion rate) state. The sources that are not persistent pulsars tend to show burst oscillations when the source is in the soft (high accretion rate) state.

This leads, as previously noted by Muno et al. (2001) and Muno, Galloway & Chakrabarty (2004), to an apparent relationship between the occurrence of burst oscillations, spin frequency, burst type, and the presence of photospheric radius expansion (PRE). Sources with burst oscillation frequency <400 Hz tend to have short, most likely helium-dominated bursts. Higher frequency sources tend to have longer bursts that probably involve mixed hydrogen/helium burning. In the soft state, short bursts are less likely to have PRE, whereas long bursts are more likely. Because burst oscillations occur more often in the soft state, the low-frequency sources are more likely to have oscillations in bursts without PRE, whereas high-frequency sources are more likely to have oscillations in bursts with PRE. The distinction is, however, not absolute, and the relationship between these various factors is clearly complex. For a more in-depth discussion of the apparent link between burst type and rotation rate, see Galloway et al. (2008).

Given that burst oscillations (for sources that are not persistent pulsars) seem to occur preferentially in certain accretion states, one can ask whether the nondetection of burst oscillations in other sources is at all surprising. Galloway et al. (2008) characterized position on the Z-shaped track in the color-color diagram using a variable $S_z$, with low values of $S_z$ corresponding to harder states and high values to softer states. For 87% of bursts with oscillations, they found $S_z > 1.75$,
Table 3  Prolific bursters without oscillations

<table>
<thead>
<tr>
<th>Source</th>
<th>Number of bursts</th>
<th>$S_z$ reported?</th>
<th>Bursts with $S_z &gt; 1.75$</th>
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<td>2E 1742.9-2929</td>
<td>84</td>
<td>N</td>
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<tr>
<td>Rapid burster</td>
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<td>N</td>
<td>...</td>
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<tr>
<td>GS 1826-24</td>
<td>65</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>Cyg X-2</td>
<td>55</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>4U 1705-44</td>
<td>47</td>
<td>Y</td>
<td>8</td>
</tr>
<tr>
<td>4U 1746-37</td>
<td>30</td>
<td>Y</td>
<td>20</td>
</tr>
<tr>
<td>4U 1323-62</td>
<td>30</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>SAX J1747.0–2853</td>
<td>23</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>EXO 1745–248</td>
<td>22</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>XTE J1710–281</td>
<td>18</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>1M 0836–425</td>
<td>17</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>SAX J1748.9–2021</td>
<td>16</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>4U 1916–053b</td>
<td>14</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>GX 17+2</td>
<td>12</td>
<td>N</td>
<td>...</td>
</tr>
<tr>
<td>4U 1735–44</td>
<td>11</td>
<td>N</td>
<td>...</td>
</tr>
</tbody>
</table>

$^a$Most burst oscillations are seen when sources are in a particular accretion state with color-color diagram position variable $S_z > 1.75$ (Galloway et al. 2008, and see their text for more detail). This table lists all sources with more than 10 bursts in the Rossi X-ray Timing Explorer Burst Catalog (for bursts up to June 3, 2007; Galloway et al. 2008) for which burst oscillations have not been detected. In most cases $S_z$ could not be computed because the source had not been observed over the full range of accretion states necessary to fully characterize the color-color diagram.

$^b$There is a tentative detection of a burst oscillation frequency for this source; see Table 2.

...
of such bursts, both involving the build-up and ignition of a thick layer of helium. Either the system is ultracompact, so that it accretes nearly pure helium (in’t Zand et al. 2005, Cumming et al. 2006), or a thick layer of helium is built up from unstable hydrogen burning at low accretion rates (Peng, Brown & Truran 2007; Cooper & Narayan 2007a). Due to their rarity, very few intermediate bursts have been observed with high time resolution instruments. Where they have been observed, no significant burst oscillation signal has been found (Linares et al. 2009, Kuulkers et al. 2010).

Burst oscillations have, however, been detected in one superburst (Strohmayer & Markwardt 2002). The source in question, 4U 1636-536, also shows burst oscillations at the same frequency in its Type I bursts. Superbursts, which last several hours, are thought to be caused by unstable carbon ignition deeper within the ocean than the Type I burst ignition point (Cumming & Bildsten 2001, Strohmayer & Brown 2002, Kuulkers 2004). The oscillations were detected over about 800 s during the peak of the 4U 1636-536 superburst, but not during the long, decaying tail. High time resolution data has only been obtained for one other superburst, from the ultracompact source 4U 1820-30. Unlike 4U 1636-536, this source has not shown burst oscillations in its Type I bursts. Unfortunately, an antenna malfunction on RXTE resulted in the loss of the high time resolution data from the peak of this superburst (Strohmayer & Brown 2002). However, no oscillations are detected during the superburst tail (unpublished analysis).

2.3.3. Frequencies. The detection of burst oscillations in several persistent and intermittent accretion-powered pulsars, sources for which the spin frequency is known, has proven conclusively that burst oscillation frequency is very close to the known spin frequency. How close, however, depends on the source. Table 4 summarizes the situation for the various persistent and intermittent accretion-powered pulsars with burst oscillations. In some cases, the frequencies agree to within $10^{-8}$ Hz, whereas for others they are separated by a few hertz.

Most burst oscillation sources exhibit frequency drift, with the frequency rising by a few hertz over the course of a burst. Although we do not have sufficient counts to resolve individual cycles, the drift can be modeled and the resulting signals can be highly coherent, with values of $Q$ as high as 4,000 (Strohmayer & Markwardt 1999). The most comprehensive study of frequency evolution in burst oscillation trains to date is that carried out by Muno et al. (2002). In most cases, the frequency drifts upward during the burst, by 1–3 Hz, to reach an asymptotic maximum (although the signal cannot always be tracked through the peak of the burst because the amplitude sometimes drops below the detectability threshold). For the two intermittent pulsars, the asymptotic maximum is 0.5–1 Hz below the spin frequency (the drifts for the regular pulsars are more unusual; see Table 4). The asymptotic maximum for a given source appears to be very stable, with the fractional dispersion in asymptotic frequencies, measured using bursts separated by several years, being $<10^{-3}$. Although orbital motion might account for some of the dispersion, it cannot account for all of the observed variation. In terms of coherence, the majority of the oscillation trains studied evolved smoothly in frequency and, hence, appeared to be highly coherent. However, in about 30% of cases, evolution was not smooth, suggesting jumps in phase or frequency, or the simultaneous presence of two signals with very similar frequencies (Muno et al. 2002).

The largest frequency drifts reported in the literature are of order a few hertz. Wijnands, Strohmayer & Franco (2001) reported an apparent drift of 5 Hz in a burst from X 1658-298, and Galloway et al. (2001) reported a drift of 3.6 Hz in a burst from 4U 1916-053. In both cases, however, the burst oscillation signal drops below the detection threshold in the middle of the burst. Because frequency cannot be tracked continuously throughout the burst, it is not clear whether we are really seeing a single signal drifting, or artificially connecting separate signals or perhaps even noise peaks (because with many bursts a few outliers due to noise would not be unexpected).
### Table 4  Comparison of burst oscillation and spin frequency

<table>
<thead>
<tr>
<th>Source</th>
<th>References</th>
<th>Frequency comparison</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Persistent accretion-powered pulsars</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>SAX J1808.4-3658</td>
<td>Chakrabarty et al. (2003)</td>
<td>Upward drift of a few hertz in the burst rise, starting below the spin frequency and overshooting. In tail, frequency exceeds spin by a few millihertz.</td>
</tr>
<tr>
<td>IGR J17498-2921</td>
<td>Chakraborty &amp; Bhattacharyya (2012)</td>
<td>The frequency of burst oscillations in the tail (they are not detected significantly in the rise) appears to be relatively stable and within ±0.25 Hz of the spin frequency. However, the precise offset, and limits on frequency drift, have yet to be quantified.</td>
</tr>
<tr>
<td>XTE J1814-338</td>
<td>Strohmayer et al. (2003); Watts, Strohmayer &amp; Markwardt (2005); Watts, Patruno &amp; van der Klis (2008)</td>
<td>Frequency is identical to the spin frequency within the errors (∼10⁻⁸ Hz) with no drifts. The exception is the brightest burst, which shows a 0.1-Hz downward drift in the burst rise.</td>
</tr>
<tr>
<td>IGR J17511-3057</td>
<td>Altamirano et al. (2010b)</td>
<td>Upward drifts of ∼0.1 Hz in the burst rise, starting below the spin frequency. There appears to be overshoot in some bursts, but whether this is significant has yet to be quantified. The frequency stabilizes very close to the spin frequency in the tail (certainly within 0.05 Hz), but the precise offset has also yet to be quantified.</td>
</tr>
<tr>
<td>IGR J17480-2446</td>
<td>Cavecchi et al. (2011)</td>
<td>Frequency is identical to the spin frequency within the errors (∼10⁻⁴ Hz) with no drifts.</td>
</tr>
<tr>
<td><strong>Intermittent accretion-powered pulsars</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Aql X-1</td>
<td>Zhang et al. (1998), Muno et al. (2002), Casella et al. (2008)</td>
<td>Burst oscillations typically drift upward in frequency during the burst. The maximum asymptotic frequency reached by the burst oscillations is 0.5 Hz below the spin frequency measured in the one brief episode where the source showed accretion-powered pulsations.</td>
</tr>
<tr>
<td>HETE J1900.1-2455</td>
<td>Watts et al. (2009)</td>
<td>Burst oscillations drift upward by ∼1 Hz during the burst, with the maximum frequency being ∼1 Hz below the spin frequency.</td>
</tr>
</tbody>
</table>

A rigorous analysis of the entire sample of burst oscillation observations, to determine limits on the size of the drifts that are compatible with the overall data set, has yet to be carried out.

In the only case where oscillations were observed in a superburst, the frequency drift was much smaller (0.04 Hz over 800 s) and entirely consistent with the expected Doppler shifts due to orbital motion (Strohmayer & Markwardt 2002). The superburst oscillation frequency inferred from this measurement was ≈0.4 Hz higher than any of the asymptotic frequencies measured during regular Type I X-ray bursts from this source (see also Giles et al. 2002). If this source shows the same behavior as that seen in the intermittent pulsars (Table 4), it is likely that the superburst oscillation frequency is closer to the true spin frequency of the star than the frequency of the normal burst oscillations.

#### 2.3.4. Amplitudes.

The average amplitudes of burst oscillations (computed over the whole burst) are highly variable, even for single sources, but are mostly in the range of 2–20% rms (Galloway...
et al. 2008). Higher average amplitudes have been measured for some bursts where the signal in the rise dominates (Strohmayer, Zhang & Swank 1997; Strohmayer et al. 1998b; Bhattacharyya & Strohmayer 2006; Galloway et al. 2008), although the error bars are larger because fewer photons can be accumulated in the short burst rise. For the oscillations detected during the superburst from 4U 1636-536, the amplitudes are ~1% rms, lower than that measured for oscillations detected in Type I bursts from this source (Strohmayer & Markwardt 2002).

Amplitudes can also vary substantially during a burst. The tendency for signals to disappear in the peaks of bursts has already been mentioned. This occurs most often, but not exclusively, during periods of photospheric radius expansion (Galloway et al. 2008) and is seen in both pulsars and nonpulsars. Significant variations in amplitude during bursts have been found for a number of sources (Muno, Özel & Chakrabarty 2002) but there are exceptions where the data are consistent with a constant amplitude model (Watts, Strohmayer & Markwardt 2005).

For the sources that are accretion-powered pulsars, one can compare the amplitudes of the burst oscillations to those of the accretion-powered pulsations (Chakrabarty et al. 2003, Strohmayer et al. 2003, Watts et al. 2009, Altamirano et al. 2010b, Cavecchi et al. 2011, Papitto et al. 2011, Chakrabarty & Bhattacharyya 2012). The burst oscillation amplitudes for the persistent pulsars are very different. However, for each individual source the burst oscillation amplitude is within a few percent of (and mostly lower than) that of the accretion-powered pulsations at the time of the burst. The difference between the amplitudes of the two types of pulsations (for at least some bursts) is statistically significant (Watts, Strohmayer & Markwardt 2005).

Harmonic content (a significant signal at the first overtone of the burst oscillation frequency) has been found in most of the burst oscillation trains from the persistent accretion-powered pulsars, although not necessarily at the same level as that seen in the accretion-powered pulsations (Chakrabarty et al. 2003; Strohmayer et al. 2003; Watts, Strohmayer & Markwardt 2005; Altamirano et al. 2010b; Cavecchi et al. 2011). Burst oscillation–only sources (Muno, Özel & Chakrabarty 2002), and burst oscillations from the intermittent pulsars (Muno, Özel & Chakrabarty 2002; Watts et al. 2009), tend not to have significant harmonic content, although see Bhattacharyya & Strohmayer (2005) for an exception in the rising phases of some bursts.

Another property that has been studied in some detail is the dependence of burst oscillation amplitude on photon energy. For burst oscillation–only sources, and burst oscillations from the intermittent pulsars, amplitude rises with energy (Muno, Özel & Chakrabarty 2003; Watts et al. 2009). For persistent pulsars where this property has been analyzed, however, burst oscillation amplitude falls with energy (Chakrabarty et al. 2003, Watts & Strohmayer 2006). For sources that show accretion-powered pulsations (persistent or intermittent) burst oscillation amplitudes have the same energy dependence as the accretion-powered pulsations, irrespective of whether this is a rise or a fall (see references above and Casella et al. 2008).

### 2.3.5. Phase offsets

Searches for phase lags between pulse profiles constructed using photons in different energy bands (energy dependent phase lags) have been carried out for several burst oscillation sources. Although in a few sources there are marginal detections of hard lags (high-energy pulse arriving later than the low-energy one), most burst oscillation profiles show no statistically significant phase offsets (Muno, Özel & Chakrabarty 2003; Watts & Strohmayer 2006; Watts et al. 2009). This differs markedly from the behavior of accretion-powered pulsations, which have significant soft lags (Cui, Morgan & Titarchuk 1998; Galloway et al. 2002; Gierliński, Done & Barret 2002; Kirsch et al. 2004; Galloway et al. 2005; Gierliński & Poutanen 2005; Papitto et al. 2010). For the persistent accretion-powered pulsars, one can also investigate phase lags between the burst oscillation pulse profile and the accretion-powered pulse profile. For XTE J1814-338, which has no detectable frequency drifts in its burst oscillations (for all but the final burst, which
occurs at much lower accretion rates and has quite different properties), the two sets of pulsations are completely phase-locked, with constant phase offset (Strohmayer et al. 2003; Watts, Patruno & van der Klis 2008). Indeed, the burst oscillation profile is actually coincident (zero phase offset) with the low-energy accretion-powered pulse profile. Spectral modeling indicates that the latter component originates from the neutron star surface (Gierliński, Done & Barret 2002; Gierliński & Poutanen 2005). Phase-locking of pulsations has also been reported for IGR J17511-3057 (Papitto et al. 2010), although frequency drifts in this source complicate this type of analysis (Altamirano et al. 2010b).

3. BURST OSCILLATION THEORIES

3.1. Relevant Physics

Burst oscillations are associated with the surface layers of the neutron star. As such, there are several key pieces of physics that must be considered when developing models for the phenomenon. Before discussing specific models, it is worthwhile reviewing these factors. Some of these intrinsic properties remain unchanged during an X-ray burst, whereas others may evolve.

3.1.1. Structure of the neutron star. Figure 3 shows the stratified composition of the surface layers of a neutron star, with ignition depths for different burst types marked. When modeling how a burst develops, one needs to take into account the coupling between the various burning

![Figure 3](image-url)

**Figure 3**

The outer layers of an accreting neutron star, showing the density $\rho$ where thermonuclear ignition takes place. Adapted from a figure from Lewin & Joss (1981).
and nonburning ocean layers, the solid crust, and the photosphere. Coupling may be dynamical, chemical, or thermal. The layers should evolve and expand due to heat generation during the burst, particularly during episodes of strong PRE (Paczynski 1983, Paczynski & Anderson 1986, in’t Zand & Weinberg 2010).

3.1.2. Heat generation and transport. Nuclear burning is unstable when the heat released by a thermonuclear reaction causes an increase in reaction rate that cannot be compensated for by cooling, resulting in a thermonuclear runaway. Several such reactions are involved in X-ray bursts. Hydrogen can burn unstably via the cold CNO cycle: $^{12}\text{C}(p, \gamma)^{13}\text{N}(\beta^+, \nu)^{13}\text{C}(p, \gamma)^{14}\text{N}(p, \gamma)^{15}\text{O}(\beta^+, \nu)^{15}\text{N}(p, \alpha)^{12}\text{C}$, where the rate-controlling temperature-dependent step is $^{14}\text{N}(p, \gamma)^{15}\text{O}$. Helium burns unstably via the temperature-dependent triple alpha reaction: $^{3}\text{He} \rightarrow ^{12}\text{C} + \gamma$. For reviews of the unstable reactions, and their application to X-ray bursts, see Schwarzschild & H"arm (1965); Hansen & van Horn (1975); Fujimoto, Hanawa & Miyaji (1981); Lewin, van Paradijs & Taam (1993); and Bildsten (1998b). Superbursts are thought to be caused by unstable burning of carbon (Woosley & Taam 1976, Taam & Picklum 1978, Brown & Bildsten 1998, Cumming & Bildsten 2001, Strohmayer & Brown 2002).

There are, however, uncertainties inherent in modeling ignition and the progression of the thermonuclear reactions that affect our understanding of the heat generation process. Ignition conditions are known to depend on accretion rate, composition of accreted material, and heat flux from the deep crust (all quantities that are impossible to measure precisely). Burning, sedimentation, and mixing between bursts are also likely to play a role (Heger, Cumming & Woosley 2007; Peng, Brown & Truran 2007; Piro & Bildsten 2007; Keek, Langer & in’t Zand 2009). Despite considerable theoretical progress in this area, there still exists a substantial mismatch between predicted and observed recurrence times for most bursters, indicating that our understanding of ignition remains poor (van Paradijs, Penninx & Lewin 1988; Cornelisse et al. 2003; Cumming 2005b; Strohmayer & Bildsten 2006; Galloway et al. 2008), although there are a few exceptions (Galloway & Cumming 2006, Heger et al. 2007). The precise details of the reaction chains are also not exactly known, despite excellent experimental work aimed at pinning this down (Schatz 2011). These uncertainties should affect not only ignition conditions but also heat generation and compositional changes throughout the burst (see, for example, Fisker et al. 2007; Cooper, Steiner & Brown 2009; Davids et al. 2011; Schatz 2011).

Heat transport is also important in models of burst oscillation development. One-dimensional simulations show that radiative heat transport should be important in all bursts, with convection also playing an important role (Woosley et al. 2004; Weinberg, Bildsten & Schatz 2006). Heat transport should also be important in determining how the thermonuclear flame spreads around the star. Multidimensional calculations and simulations have shown that convection, turbulence, conduction, and advection may all play a role (Fryxell & Woosley 1982; Spitkovsky, Levin & Ushomirsky 2002; Malone et al. 2011).

3.1.3. Rotation and flows. If burst oscillation frequency is a good measure of spin frequency (as it appears to be; see Section 2.3.3), then most burst oscillation sources rotate rapidly. Is the rotation sufficient, however, to affect the evolution of the burst? The importance of rotation in burst dynamics can be estimated by calculating the Rossby number $R_s$. This is the ratio of inertial terms to Coriolis force terms in the Navier-Stokes equations, the hydrodynamical equations governing the motions of the fluid layers where the burst takes place (see, for example, Pedlosky 1987).

$$R_s = \frac{U}{Lf},$$

Where $U$ is the angular velocity, $L$ is the characteristic length scale, and $f$ is the Coriolis parameter.
where \( U \) is the velocity of the motion, \( L \) is a characteristic length, and \( f = 4\pi \nu_{c} \cos \theta \) is the Coriolis parameter (\( \nu_{c} \) being the spin frequency of the star, and \( \theta \) the colatitude). Rotation starts to have important dynamical effects once \( R_{e} \lesssim 1 \) and the Coriolis force becomes the dominant force. This means that rotational effects must be taken into consideration once length scales exceed \( U/f \). As rotation rate increases, the effects are felt on shorter length scales. We can now estimate whether rotation is likely to affect burst oscillation mechanisms, given that oscillations have been found in stars that rotate in the range of 11–620 Hz (Table 1).

Let us first consider the effect on flame spread. One of the effects of the Coriolis force is to balance pressure gradients that develop as the hot fluid expands, hence, slowing spreading (Spitkovsky, Levin & Ushomirsky 2002). The appropriate speed for a flow driven by such pressure gradients is \( U = \sqrt{gH} \), where \( g \) is the gravitational acceleration and \( H \) is the scale height of the hot fluid. As rotation rate increases, the tendency of the Coriolis force to confine the spreading flame operates over ever shorter length scales. Significant confinement (slowing of flame spread) occurs once these are less than the size of the star, \( R \) (Cavecchi et al. 2011). This occurs for rotation rates

\[
\nu_{c} > 25 \text{ Hz} \left( \frac{g}{10^{14} \text{ cm s}^{-2}} \right)^{1/2} \left( \frac{H}{10 \text{ m}} \right)^{1/2} \left( \frac{10 \text{ km}}{R} \right).
\]

Clearly, most of the burst oscillation sources are in the regime where this is relevant.

Rapid rotation also affects oscillation modes (global wave patterns) that might develop in the ocean and atmosphere, excited by the thermonuclear burst. As above, simple estimates can be used to determine whether rotation has an effect. Shallow water gravity waves (driven by buoyancy), for example, have a timescale \( \tau = 1/N \), where \( N = \sqrt{gH} \) is the Brunt-Väisälä frequency (see, for example, Pringle & King 2007). The characteristic speed of such waves is \( U = H/\tau = \sqrt{gH} \). This means that modes with a wavelength \( \lambda \) comparable to or larger than \( \sqrt{gH}/f \) should be sensitive to the effects of rotation. Large-scale global modes (those with the largest wavelengths, \( \lambda \sim R \)) are therefore likely to be affected by rotation for most of the burst oscillation sources (compare to Equation 7).

Rotation can also affect ignition conditions. Rotation lowers the effective gravity \( g_{\text{eff}} \) at the equator as compared to the poles, with the difference being given by

\[
\frac{\delta g_{\text{eff}}}{g_{\text{eff}}} \sim \left( \frac{\Omega_{e}}{\Omega_{c}} \right)^{2} \sim 5\% \left( \frac{\nu_{c}}{500 \text{ Hz}} \right)^{2} \left( \frac{R}{10 \text{ km}} \right)^{1/3} \left( \frac{1.4 \text{ M}_{\odot}}{M} \right),
\]

where \( \Omega_{c} \) is the Keplerian angular velocity at the surface of the neutron star. The reduced gravity leads to a higher rate of fuel accumulation at the equator: Because of this, ignition is likely to occur preferentially at equatorial latitudes for all but a small range of accretion rates (Spitkovsky, Levin & Ushomirsky 2002; Cooper & Narayan 2007b).

The expansion associated with the X-ray burst could also, in principle, lead to differential rotation or shearing flows. Calculations show that the change in thickness of the burning layers as they expand during a burst is \( \Delta R \sim 20 \text{ m} \) (Bildsten 1998b). If angular momentum were conserved, this would lead to a spin down of order

\[
\Delta \nu_{c} \approx \frac{2\nu_{c} \Delta R}{R} = 2 \text{ Hz} \left( \frac{\nu_{c}}{500 \text{ Hz}} \right) \left( \frac{\Delta R}{20 \text{ m}} \right) \left( \frac{10 \text{ km}}{R} \right).
\]

Over the course of the burst, the hot layer could, in principle, achieve multiple wraps of the underlying star. Zonal flows (latitudinal differential rotation involving east-west flow along latitude lines, as opposed to meridional flows, which involve north-south flow along longitude lines) may also develop due to temperature gradients as different latitudes ignite at different times (Spitkovsky, Levin & Ushomirsky 2002). In practice, any shear flow (radial or latitudinal) would be attenuated...
by various frictional processes or shearing instabilities, for instance. However, if shear flows do persist, they will affect the hydrodynamics of the surface layers, modifying, for example, the structure and stability of oscillation modes (Pringle & King 2007).

3.1.4. Magnetic fields. Measuring magnetic field strength for the burst oscillation sources is very difficult. For some of the pulsars, it has been possible to put limits on field strength by observing spin-down between accretion episodes and calculating the field strength necessary for this to occur via magnetic dipole radiation. Using this method it has been determined that the accretion-powered pulsar SAX J1808.4-3658, for example, has a field $\sim 10^8$ G (Hartman et al. 2008, 2009). Most of the burst oscillation sources, however, are not pulsars. If we assume that this is because the magnetic field is too weak to cause channeled accretion at the observed accretion rates, then this sets an upper limit on field strength of $\sim 10^9$ G (for a discussion of the techniques used in making this type of estimate, see Psaltis & Chakrabarty 1999). It is possible, however, that the magnetic field is simply aligned with the rotation axis (Chen & Ruderman 1993) or that pulsations are obscured (Titarchuk, Cui & Wood 2002; Göğüş, Alpar & Gilfanov 2007).

The importance of magnetic fields on the dynamics of the burning layers can be estimated by calculating the ratio of the Lorentz force terms to the other force terms in the magnetohydrodynamic versions of the Navier-Stokes equations. The magnetic contribution is often split into two terms, a magnetic pressure and a magnetic tension (see, for example, Choudhuri 1998). It should also be borne in mind that the field is unlikely to remain static during the burst. Flows set up by the burst (convection, spreading of fuel or flame front, or shearing due to differential rotation) may lead to amplification and modification of the field (Cumming & Bildsten 2000; Boutloukos, Miller & Lamb 2010). Although magnetic pressure is unlikely to be relevant compared to other pressure terms at the burning depth, it will dominate in the very outermost layers of the atmosphere. Magnetic tension, which can act to counterbalance pressure gradients associated with accumulating fuel and flame spread, may be dynamically important (Brown & Bildsten 1998, Cavecchi et al. 2011). Magnetic fields also introduce new types of oscillation and instability in the ocean layers [see Choudhuri (1998) for a general overview of magnetohydrodynamic oscillations, Heng & Spitkovsky (2009), and Section 3.2.2]. Magnetic fields also affect conditions in the ocean layers even prior to ignition. Channeling of accreting material onto the magnetic poles of the neutron star may lead to a local overdensity at the magnetic polar caps as well as lead to temperature and composition gradients (Brown & Bildsten 1998).

3.2. Current Models for Burst Oscillations

Current models for burst oscillations fall into two categories, hot spot models and global mode models, and these are illustrated in very general terms in Figure 4. As is discussed in detail below, it seems likely that burning spreads initially from an ignition point, forming a spreading hot spot in the rising phase of the burst. The burning front then either stalls, to leave a persistent hot spot, or spreads around the star, exciting large-scale waves in the ocean. Both could lead to a brightness asymmetry in the ocean during the tail of the burst. We treat each class of model in turn, noting that they may not be mutually exclusive.

3.2.1. Hot spot models. Hot spot models are based on the general principle that the thermonuclear burning is not occurring uniformly across the surface of the star, but is instead confined to a smaller region. This hot spot is then modulated by the star’s rotation to give rise to the observed burst oscillations. Two types of hot spot models have been considered: spreading hot spots, generated temporarily in the rise as the burst ignites and flame spreads from the ignition site to engulf
Burning spreads from ignition location

**Figure 4**

Simplified schematic of current burst oscillation models. Burst oscillations require the presence of a brightness asymmetry that can be modulated by the star’s rotation so that the observer sees pulsations at close to the spin frequency. (a) Ignition is expected to start at a point; a flame front follows and then spreads across the star (red, hot; blue, cold). This is known as a spreading hot spot. What happens then is unclear. One possibility is that (b) the flame front stalls, so that only part of the ocean burns, leaving a hot spot that persists in the tail of the burst. The other possibility is that (c) the flame front spreads around the star and excites large-scale waves (global modes) in the ocean. The peaks and troughs of the waves differ in temperature so that the wave pattern gives rise to a brightness asymmetry.

the star, and persistent hot spots caused by restriction of the burning to a small part of the stellar surface.

In the tails of most bursts, the blackbody radius obtained from fitting the overall burst spectrum is comparable to the radius of the star, implying that the flame has engulfed the entire surface (see, for example, Galloway et al. 2008). However, it takes hours to days to accumulate fuel between bursts, and less than a second for a thermonuclear runaway to develop (Shara 1982). For ignition conditions to be met simultaneously across the stellar surface, the thermal state would need to be consistent to better than one part in \( \sim 10^4 \) (Cumming & Bildsten 2000). The presence of slight asymmetries in accretion (due, for example, to magnetic channeling or the presence of equatorial boundary layers) makes this unlikely—particularly for the accretion-powered pulsars. In the absence of a mechanism that could equalize the thermal state of the ocean to the required level, it is therefore assumed that ignition starts at a point and that a flame front then spreads across the stellar surface.

The presence of such a spreading hot spot would provide a simple explanation for the presence of burst oscillations in the rising phase of bursts. Results from a small sample of bursts appear to support this picture: In a few bursts that have strong oscillations in the rising phase, the amplitude of oscillations falls as the blackbody radius of the overall burst spectrum increases (Strohmayer, Zhang & Swank 1997; Strohmayer et al. 1998b; Bhattacharyya & Strohmayer 2006). This is consistent with the idea of a flame front spreading to cover the star, because as the spot grows in
size, the overall amplitude of pulsations will fall (Muno, Özel & Chakrabarty 2002). There are, however, several problems and theoretical questions that then arise.

The first issue is that if point ignition and flame spread are occurring in all bursts, why do we not detect oscillations in the rising phase of all bursts? As discussed in Section 2.3.2, oscillations are actually more common in the tails rather than the rising phase of bursts. One possibility is that this is a detection bias: It can be difficult to make detections in the rising phase of bursts given their short duration. Something that has yet to be done is a comprehensive study to check whether the current data, including upper limits, are consistent with the spreading hot spot model.

One factor that also affects detectability is the latitude at which ignition occurs. On a rapidly rotating star, ignition is expected near the equator for most accretion rates due to the lower effective gravity, which makes it easier to build up the column depth of material necessary for ignition (Spitkovsky, Levin & Ushomirsky 2002). There are, however, small ranges of accretion rate close to the boundary between stable and unstable burning where ignition is expected to occur at higher latitudes (Cooper & Narayan 2007b). Whether a burst ignites at the equator or at higher latitudes can have a major effect on the detectability of burst oscillations (Maurer & Watts 2008). For sources with a substantial amount of magnetic channeling, ignition may also occur preferentially at the magnetic poles due to local overdensities or extra heating (Watts, Patruno & van der Klis 2008).

How the flame then spreads is equally important to burst oscillation detectability because the flame must be able to spread in such a way that an azimuthal asymmetry can persist. The processes controlling flame spread in X-ray bursts have been an open question for years, with various heat transfer mechanisms including conduction, turbulence, and convection, which are all thought to play a role (Fryxell & Woosley 1982; Nozakura, Ikeuchi & Fujimoto 1984; Bildsten 1995; Zingale et al. 2001). Spitkovsky, Levin & Ushomirsky (2002) also pointed out the importance of hydrodynamical effects, in particular the interaction between the Coriolis force and expansion of the hot burning material. The Coriolis force acts to slow down flame spread, thereby preserving a hot spot. Indeed some degree of confinement may be essential to get the flame front established and propagating because rapid expansion and lateral spread of the hot material might otherwise cause the flame to stall (Zingale et al. 2003). Note, however, that Coriolis force confinement is not effective for IGR J17480-2446, which has a rotation rate of only 11 Hz (see Section 3.1.3 and Cavecchi et al. 2011). The flame spread mechanism remains an unsolved problem with immense importance for burst oscillation models.

If the flame spreads across the whole star during the rising phase, the spreading hot spot dissipates. The fact that different regions of the star ignite at different times leaves some residual temperature asymmetry in the tail. However, the magnitude of the predicted difference is too low to explain the amplitudes of the burst oscillations observed in burst tails (Cumming & Bildsten 2000). Some additional mechanism, or modification to the model, is still required. One possibility is the excitation of large-scale waves (Section 3.2.2). The other is that a hot spot survives because the burning front does not spread across the whole star.

One way in which this might occur is if fuel is confined, with the prime candidate for a confinement mechanism being the star’s magnetic field. Matter channeled onto the magnetic polar caps of the star will be prevented from crossing field lines (and, hence, flowing across the star) until the overpressure is sufficiently large to deform the field lines. Estimates by Brown & Bildsten (1998) show that for matter to remain confined in the ignition depth for normal Type I bursts requires fields of at least $10^{10}$ G, which is much higher than the field strengths estimated for the burst oscillation sources (Section 3.1.4). Magnetohydrodynamical instabilities may also act to make magnetic confinement of fuel ineffective (Litwin, Brown & Rosner 2001). Magnetic fuel confinement on burst oscillation sources is therefore expected to be relatively unlikely.
The alternative is that the flame front itself is confined: Burning, once started, spreads some distance and then stalls. This requires heat transport to be impeded in some way. Several mechanisms have been explored in the literature. Payne & Melatos (2006) suggested that magnetic field evolution on an accreting neutron star might result in the development of strong magnetic belts around the equator that would then impede north-south heat transport. On rapidly rotating stars, a reduction in Coriolis-mediated confinement as the flame front tries to cross the equator might result in stalling (Spitkovsky, Levin & Ushomirsky 2002; Zingale et al. 2003). Both of these mechanisms would confine burning to one hemisphere of the star: It is unclear whether this would lead to an asymmetry of sufficient magnitude to explain burst oscillation amplitudes. Recently Cavecchi et al. (2011) showed that the dynamical interaction between the expanding burning fuel and the radial magnetic field could, in principle, induce horizontal field components that might be large enough to restrict further spread. This would lead to more localized confinement. For this mechanism to work the initial field can, in principle, be somewhat lower than for fuel confinement, $\sim 10^9$ G (consistent with estimates for two sources, XTE J1814-338 and IGR J17480-2446). If ignition starts at the magnetic pole, this would result in burst oscillations that are phase-locked to the accretion-powered pulsations and have only minimal frequency drift, consistent with observations from these two sources (Sections 2.3.3 and 2.3.5). This mechanism may not work, however, for sources that appear to have lower magnetic fields unless something in the burst process (such as a convective dynamo) acts to increase the field temporarily (Boutloukos, Miller & Lamb 2010).

A major question addressed even in the earliest papers on burst oscillations was how to explain the upward frequency drift seen in most bursts (Section 2.3.3). Strohmayer, Zhang & Swank (1997) pointed out that horizontal motion of the spreading flame front could lead to drifts in frequency of a few hertz. However, in this case rotation would have to set a preferred direction for spread to explain why the frequency always tends to rise. They therefore suggested an alternative possibility: that of angular momentum conservation during vertical expansion of the heated burning layers. Rapid expansion would cause a hot spot to rotate more slowly, giving an observed frequency below the spin rate, with frequency rising as the layers cooled and contracted again (see Section 3.1.3). The expansion model depends on two key assumptions: (a) that the burning layers can decouple from the underlying star and (b) that shearing within the burning layer itself is small enough to preserve the spot rather than cause it to be smeared out. The validity of these assumptions and the magnitude of the expected frequency shift in first Newtonian gravity and then General Relativity were examined by Cumming & Bildsten (2000) and Cumming et al. (2002). These researchers examined a range of hydrodynamical coupling mechanisms, such as viscous or shearing instabilities, and found that it was, in principle, possible for the burning layer to remain decoupled for the timescale of the burst. Smearing out of the hot spot was more problematic, and keeping this coherent required convection or short wavelength baroclinic instabilities operating inside the burning layer. Smearing was found to be particularly pronounced during episodes of PRE. The maximum frequency drifts predicted by these studies were $\sim 1$–2 Hz. Although larger drifts have been reported, as explained in Section 2.3.3 the largest drifts in the literature are not clear cut, and the data set as a whole may in fact be consistent with a smaller maximum drift. Magnetic wind-up and shearing effects may also be important in determining the coupling and angular momentum transfer between the expanding layers and the underlying star (Cumming & Bildsten 2000; Lovelace, Kulkarni & Romanova 2007). A role for the magnetic field may explain the different drift properties seen in burst oscillations from the accretion-powered millisecond pulsars, where the magnetic field is known to be dynamically important.

### 3.2.2. Surface modes

Ignition of the burst and the subsequent spread of flame around the star may excite large-scale waves (global modes) in the neutron star ocean. Height differences
associated with such oscillations would translate into hotter and cooler patches (the wave pattern), thus giving rise to differences in X-ray brightness. Nonaxisymmetric modes could, in principle, be excited easily by the initial flame spread and persist throughout the burst tail (depending on damping mechanisms).

The problem of finding global modes of oscillation in oceans is one with a long and venerable history, due to its applications to Earth’s oceans. As such, papers on this topic use a rich and sometimes confusing mix of terminology when referring to different mode types. The basic hydrodynamical equations of continuity (mass conservation), momentum, and energy, applied to the oscillations of a shallow stably stratified ocean on a rotating sphere, reduce to what is known as Laplace’s tidal equation (Longuet-Higgins 1968, Lou 2000, Townsend 2005). The restoring forces in this simple system are buoyancy (due to temperature or composition gradients) and the Coriolis force.

Nonaxisymmetric mode solutions to Laplace’s tidal equation have dependence \( \exp(im\phi) \) on the azimuthal angle \( \phi \), where \( m \) is an integer. Given a mode with an azimuthal number \( m \) and frequency \( \nu \) in the rotating frame of the star, the frequency \( \nu_o \) seen by an inertial observer would be

\[
\nu_o = m\nu_s + \nu_r,
\]

where \( \nu_s \) is the spin frequency of the star, and the sign of \( \nu_r \) is positive or negative depending on whether the mode is prograde (eastbound) or retrograde (westbound), respectively. The angular structure of the modes, which depend on spherical harmonics, are characterized by the usual integers \( l \) and \( m \) (see, for example, Mathews & Walker 1970). The pattern has \( m \) nodes in azimuth and \( |l-m| \) nodes in latitude. For nonzero \( \nu_r \), the brightness pattern moves around the star, permitting an offset from the spin-frequency. Frequency drift can be naturally explained if \( \nu_r \) depends on the thermal state of the ocean, because this changes as the burst evolves and cools through the tail.

Laplace’s tidal equation admits three families of mode solution:

- **Poincaré modes**: propagate in the retrograde (westbound) direction and reduce to pure gravity waves (restored by buoyancy alone) in the nonrotating limit. For this reason, they are often referred to as g-modes in the neutron star ocean oscillation literature (see, for example, Bildsten, Ushomirsky & Cutler 1996 and Heyl 2004).
- **Kelvin modes**: propagate in the prograde (eastbound) direction and also reduce to pure gravity waves in the nonrotating limit. Unlike the Poincaré modes, they are in geostrophic balance. This means that the horizontal component of the Coriolis force balances the horizontal pressure gradient (see Pedlosky 1987). As a result, they involve purely azimuthal motions and are confined to an equatorial waveguide.
- **Rossby modes**: propagate in the retrograde (westbound) direction and are also known as r-modes (Papaloizou & Pringle 1978a, Saio 1982). In the limit of zero buoyancy, Rossby modes are driven purely by latitudinal variations in the Coriolis force. In the nonrotating limit, they reduce to trivial zero-frequency solutions. If buoyancy is present, then it will also act to restore these modes, and they are then often referred to as buoyant r-modes (see, for example, Heyl 2004 and Piro & Bildsten 2005b).

Heyl (2004) was the first to give serious consideration to whether such ocean modes might explain the properties of burst oscillations, particularly in the tails of bursts. He laid out a number of criteria that the modes would have to meet, including the fact that observed frequency should be a few hertz below the spin frequency of the star, and that low \( l, m \) modes would be needed to ensure that a highly sinusoidal and high-amplitude burst oscillation would result (the finer the pattern, the lower the contrast across the stellar surface). On the basis of these criteria, he determined
that the \( l = 2, m = 1 \) buoyant r-mode was the most likely candidate. This retrograde mode has \(|\nu_r|\) of only a few hertz, giving an observed frequency slightly below the spin frequency. As the burning layers cool (changing the buoyancy), \(|\nu_r|\) gets smaller, so that observed frequency would tend toward the spin frequency. Poincaré or g-modes were ruled out primarily on the grounds of their frequencies because \(|\nu_r|\) is expected to be much larger than a few hertz (McDermott & Taam 1987; Bildsten & Cutler 1995; Bildsten, Ushomirsky & Cutler 1996; Strohmayer & Lee 1996; Bildsten & Cumming 1998; Heyl 2004; Maniopoulou & Andersson 2004). Kelvin modes were ruled out on the grounds that they are prograde, so that frequency would fall as the ocean cooled, in contrast to the majority of observed frequency drifts. Both Kelvin and Poincaré modes are also strongly confined to the equatorial regions on rapidly rotating stars, which would reduce overall burst oscillation amplitudes (because there is no strong contrasting mode pattern across most of the surface). The buoyant r-mode, by contrast, occupies a wider band around the equator, giving greater contrast.

In addition to providing a natural explanation for the sinusoidal shape, overall frequency, and amplitude of the burst oscillations, mode models predict that the amplitude of the burst oscillation should increase with photon energy (Heyl 2005, Lee & Strohmayer 2005, Piro & Bildsten 2006), in line with observations of the nonpulsars and the intermittent pulsars (although not those of the persistent pulsars). Heyl (2004) also argued that excitation of such a mode should be relatively easy because the timescale of the mode matches the \( \sim 1 \)-s rise time of the burst associated with the flame spread. Narayan & Cooper (2007) and Cooper (2008) explored the issue of excitation in more detail, concluding that the mode would need to be unstable in order to grow to the required amplitudes in the tails of bursts. They considered various classical pumping mechanisms (Saio 1993) and conclude that the main driver is likely to be the \( \epsilon \) mechanism, which drives modes via nuclear energy generation. The role of the \( \epsilon \) mechanism in neutron star envelopes was studied previously by McDermott & Taam (1987) and Strohmayer & Lee (1996) for thermally unstable envelopes. Narayan & Cooper (2007) and Cooper (2008), by contrast, consider thermally stable envelopes, appropriate for the tails of bursts. For He-rich explosions, instability is more likely when the burst is radiation-pressure dominated. Instability was much less likely to develop in H-rich bursts. Suppression of the instability occurs during episodes of convection, which may contribute to the observed disappearance of burst oscillations during the peaks of bright photospheric radius expansion bursts.

The major problem with the buoyant r-mode model is that the frequency drift predicted as the burning layer cools is \( \sim 10 \) Hz, an order of magnitude larger than the observed values. At \( 10^9 \) K, a typical temperature in the peak of a burst, the buoyant r-mode frequency should be \(|\nu_r| \gtrsim 10 \) Hz, drifting to \(|\nu_r| \sim 1 \) Hz as the layer cools to \( 10^8 \) K. Various solutions to this problem have been explored. Piro & Bildsten (2005a) pointed out the existence of another global mode of oscillation that is confined to the interface between the cool ocean below the burning layer and the underlying elastic crust. The observed frequency of this crust-interface mode would be \( \sim 4 \) Hz below the spin frequency of the star. If, as the buoyant r-mode drifted upward in frequency, it could couple efficiently to this crust-interface mode and transfer its energy via resonant conversion, this would naturally truncate the drift a few hertz short of the spin frequency (Piro & Bildsten 2005b). The frequency of the crust-interface mode is highly stable and, thus, could account for the reported invariance in asymptotic frequencies. It could also explain why the burst oscillation frequency seen in a superburst is close to that seen in normal bursts, despite the differences in the burning layer, because the final frequency in both cases would be set by the crust-interface mode. Unfortunately, detailed studies of the coupling between the buoyant r-mode and the crust-interface wave indicate that resonant conversion is not effective (Berkhout & Levin 2008). The fact that the separation between spin frequency and burst oscillation frequency is much less than
4 Hz for the accretion-powered pulsars (Table 4) is also problematic for the crust-interface mode model.

As a result, several alternative models have been explored. Heyl (2004) pointed out that if the r-mode were instead confined to the photospheric layers, the drift would be smaller. This idea has yet to be explored in detail, but as pointed out by Berkhout & Levin (2008), magnetic forces become important in these low-density layers and could have a substantial effect on mode frequencies. Cumming (2005a) explored what might happen to the buoyant r-modes if strong zonal flows (latitudinal differential rotation) were to develop in the ocean layers in the immediate aftermath of flame spread. Although shear-modified modes could, in principle, match both frequencies and drifts, his study showed that high \( m \) modes were likely to grow much faster than the low \( m \) modes necessary to explain burst oscillation properties. Whether zonal flows can develop in the first place is also still an open question (Spitkovsky, Levin & Ushomirsky 2002). Most recently, Heng & Spitkovsky (2009) considered the effects that magnetic fields might have on oceanic mode structure by solving the shallow water magnetohydrodynamical equations for an incompressible ocean with a purely radial magnetic field. In addition to magnetically modified versions of the normal families of modes described above, they find new solutions dominated by magnetic and rotational effects that they call magnetostrophic modes. Unlike the previously known modes, which are confined to the equatorial regions on a rapidly rotating star, these new modes are stronger near the poles. Both prograde and retrograde modes are possible; however, the model predicts a downward rather than an upward frequency drift for the retrograde modes as the ocean cools. More detailed calculations, however, are required to determine whether or not magnetically modified modes such as these might play a role in explaining burst oscillations.

Mode models remain an extremely promising mechanism to explain burst oscillations from the nonpulsars and the intermittent pulsars, although issues such as the frequency drift problem remain to be resolved. For the persistent accretion-powered pulsars, the models have more difficulty: existing mode models cannot explain the extremely close agreement between spin and burst oscillation frequency (Table 4), which would require \( |\nu_r| \ll 1 \text{ Hz} \) for an \( m = 1 \) mode; the unusual frequency drifts (or lack thereof); and the fact that burst oscillation amplitude decreases with photon energy. Magnetically modified modes may eventually account for these differences; alternatively, sources with a dynamically important magnetic field may have a different burst oscillation mechanism (such as a magnetically confined hot spot; see Section 3.2.1).

4. USES OF BURST OSCILLATIONS

Burst oscillations are an intrinsic part of the thermonuclear burst process. They can also, however, be used as tools to explore other areas of neutron star physics. In this Section, I expand briefly on some of these applications.

4.1. Pulse Profile Modeling as a Diagnostic of Mass and Radius

The nature of the strong force, and the state of matter at extremes of temperature and density, is an extremely active field of research. Of particular interest is the transition from nucleons (neutrons and protons) to deconfined quarks and gluons or other more exotic states. At low densities, this can be studied via experiments like the Large Hadron Collider or in various heavy ion experiments such as the Relativistic Heavy Ion Collider and the Facility for Antiproton and Ion Research. At higher densities, however, neutron stars are the only environment in the Universe where the transition can be explored (Paerels et al. 2009).

Dense matter models, combined with the relativistic stellar structure equations, make predictions for mass and radii of neutron stars. By measuring these quantities, we can work back to
The underlying nuclear physics (Lattimer & Prakash 2007). Burst oscillations are expected to be powerful tools in this regard because the emission comes from the surface of the neutron star, deep within the gravitational potential well. As photons propagate toward us, they are affected by relativistic effects that depend on mass and radius, such as gravitational redshift and lightbending. The pulse profile associated with the surface emission pattern is modified by these processes. By modeling the shape and energy dependence of the observed pulse profile using relativistic ray-tracing algorithms, researchers seek to deconvolve these effects and, hence, extract information about mass and radius. Typically, one has to fit for the surface emission pattern and the geometry (such as observer inclination), as well as the parameters of interest.

The fact that stellar compactness affects pulse profiles from a hot spot on the surface of the neutron star is long-established, and a series of papers explore the effects of (for example) different metrics, rotation, and stellar oblateness (Pechenick, Ftaclas & Cohen 1983; Chen & Shaham 1989; Strohmayer 1992; Braje, Romani & Rauch 2000; Poutanen & Gierliński 2003; Cadeau, Leahy & Morsink 2005; Cadeau et al. 2007; Morsink et al. 2007). The techniques developed in these papers are generic to all types of hot spots and have been applied extensively to accretion-powered pulsations as well as burst oscillations. Following the discovery of burst oscillations, several researchers started to model the lightcurves and pulse profiles that might be expected from both static and spreading hot spots or mode patterns on the surface of bursting neutron stars (Strohmayer, Zhang & Swank 1997; Miller & Lamb 1998; Weinberg, Miller & Lamb 2001; Muno, Özel & Chakrabarty 2002, 2003; Viironen & Poutanen 2004; Lee & Strohmayer 2005). Some attempts were also made at the inverse problem, that of fitting measured burst oscillation pulse profiles in order to obtain confidence contours on stellar compactness (Nath, Strohmayer & Swank 2002; Bhattacharyya et al. 2005). Many more attempts have been made to obtain constraints by fitting accretion-powered pulsations, despite the complicating effects of the accretion funnel and shock on the emission (see Poutanen 2008 for a review). Burst oscillations offer, in principle, a somewhat cleaner system dominated by thermal emission. Although the constraints obtained using existing data were relatively weak, the potential of the technique to put tight bounds on mass and radius, given sufficient photons, was clear (Strohmayer 2004). As such, pulse profile modeling of burst oscillations is now a major science driver for proposed future large-area X-ray timing missions such as the Large Observatory for X-ray Timing (Feroci et al. 2012) and the Advanced X-ray Timing Array (Ray et al. 2010). A concerted effort is now under way to address and resolve some of the outstanding issues that may introduce degeneracies into fits for mass and radius, such as the effect of changes in the surface emission pattern over the course of a burst.

4.2. Neutron Star Spin

The evidence outlined in Section 2.3.3 supports the identification of burst oscillation frequency as a good measure of neutron star spin, at least to within a few hertz. The main consequence of this has been to double the number of rapidly-rotating (above 10 Hz) accreting neutron stars with a known spin rate. Indeed, the fastest spinning accreting neutron star currently known (4U 1608-522, with a spin of 620 Hz) is a burst oscillation source and not an accretion-powered pulsar.

Identifying the spin distributions of the various classes of neutron star has been a long-standing research goal for many years, as they are an important element in our understanding of stellar and binary evolution. The discovery of rapidly rotating accreting neutron stars, in particular, was regarded as critical to confirming the recycling scenario for the formation of the millisecond radio pulsars (Alpar et al. 1982, Radhakrishnan & Srinivasan 1982, Bhattacharya & van den Heuvel 1991). With a larger number of stars in this class, more detailed studies of population evolution are possible, revealing interesting discrepancies between models and observation (Tauris & van...
den Heuvel 2006, Lorimer 2008, Hessels 2008, Kiziltan & Thorsett 2009, Tauris 2011). These point to problems in our understanding of, for example, the mass transfer process, magnetic field decay, and accretion torques. Other formation routes for millisecond radio pulsars, such as accretion-induced collapse of white dwarves, may also need to be invoked to explain the observed populations.

The maximum spin rate that a neutron star can reach is also of great interest. A neutron star with a submillisecond spin period would place a tight and very clean constraint on the dense matter equation of state (Lattimer & Prakash 2007, Schaffner-Bielich 2008, Haensel et al. 2009). This is because the break-up, or mass-shedding, frequency (the spin rate above which a neutron star would fly apart as rotational forces overwhelm gravitational attraction) depends strongly on the composition of the star. This, in turn, depends on the poorly constrained behavior of the strong force at supranuclear densities. Although no current burst oscillation source (and indeed not even the most rapidly rotating radio pulsar; Hessels et al. 2006) rotates fast enough to rule out equations of state, the search for extremely rapid rotators does motivate burst oscillation searches. Whether burst oscillations could ever develop, or be detectable, on such rapidly rotating stars remains, however, an open question (see Section 3.1.3).

The current spin distribution of accreting neutron stars, as given by both the accretion-powered pulsars and the burst oscillation sources, hints at a maximum that is well below the spin rate suggested by simple estimates of accretion-induced spin-up over their lifetime (Chakrabarty et al. 2003, Chakrabarty 2008). If the evolutionary estimates are sound, there is a requirement for a braking mechanism to halt the spin-up. Magnetic braking (due to interaction between the stellar field and the accretion disk) is one possibility (Ghosh & Lamb 1978, White & Zhang 1997, Andersson et al. 2005). Another, which has generated a lot of excitement, is the emission of gravitational waves (Papaloizou & Pringle 1978b, Wagoner 1984, Bildsten 1998a). This has triggered major theoretical effort exploring the nature of possible gravitational wave generation mechanisms, such as crustal mountains (Bildsten 1998a; Ushomirsky, Cutler & Bildsten 2000; Melatos & Payne 2005; Haskel, Jones & Andersson 2006), or internal r-mode oscillations (Bildsten 1998a; Andersson, Kokkotas & Stergioulas 1999; Levin 1999; Andersson et al. 2000; Andersson, Jones & Kokkotas 2002; Heyl 2002; Wagoner 2002; Nayyar & Owen 2006; Bondarescu, Teukolsky & Wasserman 2007; Ho, Andersson & Haskell 2011). Gravitational wave braking could also make accreting neutron stars promising continuous wave sources for future gravitational wave detectors, although this is one application where knowing the spin to a very high degree of precision (certainly better than a few hertz) would be important (Watts et al. 2008). Uncertainty in the spin rate has a very negative impact on the gravitational wave detection threshold because increasing the parameter space increases the number of trials (reducing detection sensitivity; see Section 2.1) and increases the computational power needed to perform any search. Improving burst oscillation models so that we can make a more accurate diagnosis of spin rate would be of great benefit.

5. CONCLUSIONS

Burst oscillations are an intriguing part of the phenomenology of thermonuclear bursts on neutron stars, with wider uses in terms of measuring stellar spin and potentially constraining the dense matter equation of state. One of the legacies of the RXTE has been a rich database of burst oscillation observations, giving us a clear understanding of their general properties and the conditions under which they develop. A satisfactory theoretical explanation of why and under what conditions burst oscillations develop, however, is still lacking. Burst evolution models that take full account of the structure of both the neutron star ocean and envelope, and the dynamical effects of magnetic fields, are needed to explore the mechanics of flame spread and the excitation
of global oceanic modes. Such theoretical development is essential if we are to take full advantage of the opportunities offered by the next generation of X-ray timing telescopes.

**DISCLOSURE STATEMENT**

The author is not aware of any affiliations, memberships, funding, or financial holdings that might be perceived as affecting the objectivity of this review.

**ACKNOWLEDGMENTS**

A.L.W. acknowledges support from a Netherlands Organisation for Scientific Research (NWO) Vidi Fellowship. She thanks Michiel van der Klis and Deepto Chakrabarty for their encouragement and feedback while writing this review. She also thanks Diego Altamirano, Tullio Bagnoli, Yuri Cavecchi, Duncan Galloway, Yuri Levin, and Jean in’t Zand for their comments on the draft manuscript.

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